

# CP Parameters of the $B^0_s$ at the Tevatron

Joe Boudreau

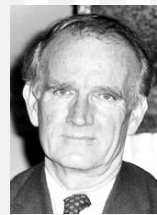
For the CDF and D0 collaborations

Montpellier QCD Workshop

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# CP Violation

- Study of CP symmetry and its violation is a strong hint to the underlying dynamics of particle interactions.

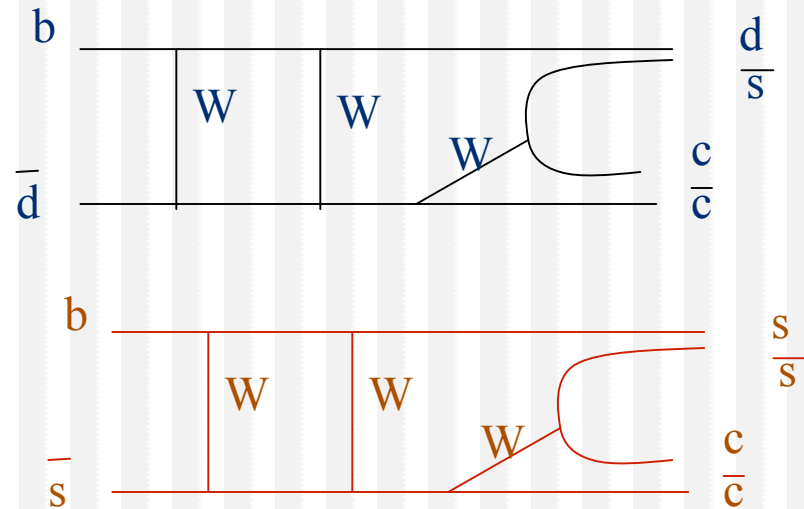


- A great example: Cronin & Fitch's discovery of CP violation in 1964 indicates (Kobayashi, Maskawa 1973) three generations of quarks.
- BSM CP violation in the  $B_s^0$  sector could indicate a fourth generation (see [arXiv:0803.1234v3](#))
- Fascinating connection to cosmology, since the standard model has all of the ingredients to generate an  $O(10^{-20})$  Baryon Asymmetry of the Universe  $n_b/n_\gamma \sim 10^{-20}$ , namely the three Sakharov conditions of **baryon number violation**, **CP violation**, and **departure from thermal equilibrium**. However  $n_b/n_\gamma$  measured to be  $O(10^{-10})$ .

# CP violation in the $B^0_s$ system

- The Tevatron produces all species of b-hadrons:  $B^0$ ,  $B^+$  but also  $B^0_s$ ,  $B_c^+$ ,  $\Lambda_b$  ( $\Sigma_b$ ,  $\Xi_b$ ,  $\Omega_b$ ...) excited states
- In the  $B^0_s$  sector, two measurements stand out, because one can compare clean measurements to precise theory predictions:
- The measurement of the CP phase  $\beta_s$  in the decay of  $B^0_s \rightarrow J/\psi \phi$ 
  - New measurement from CDF based on  $5.2 \text{ fb}^{-1}$ ; older ( $2.8 \text{ fb}^{-1}$ ) measurements from D0
- The measurement of the semileptonic CP asymmetry  $A_{sl}^b$ 
  - New measurement of the dilepton charge asymmetry from D0 ( $6.1 \text{ fb}^{-1}$ ); older ( $1.6 \text{ fb}^{-1}$ ) measurement from CDF.
- These both involve mostly the physics of the weak interaction.

The decay  $B_s^0 \rightarrow J/\psi \phi$  measures a CP phase similar to the angle  $\beta$  measured in  $B^0 \rightarrow J/\psi K^0$  decay: we replacement a d antiquark by an s antiquark



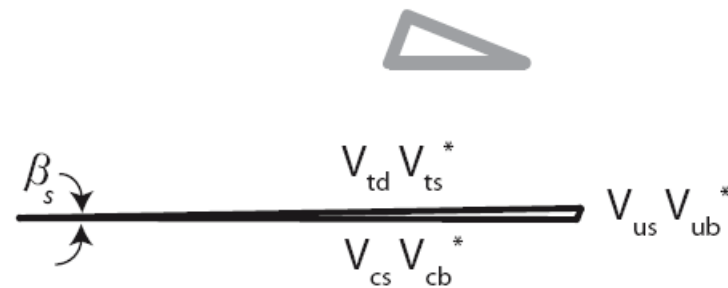
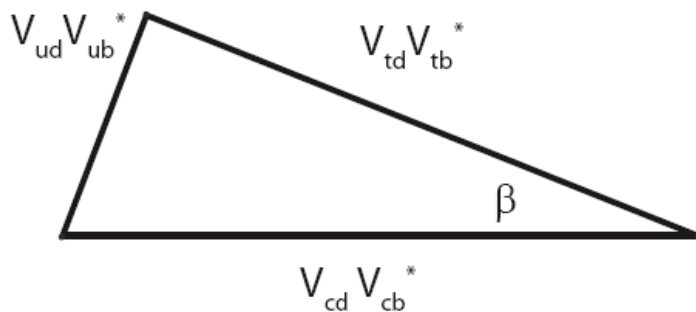
$B^0 \rightarrow J/\psi K^0$

$$\begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

$B_s^0 \rightarrow J/\psi \phi$

$$\begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

We are measuring not the (bd) unitarity triangle but the (bs) unitarity triangle:





$$B^0_s \rightarrow J/\psi \phi$$

- $B^0_s \rightarrow J/\psi \phi$  is **two** particles decaying to **three** final states..

Two particles:

$$|B^0_{S,L}\rangle = p|B^0_S\rangle + q|\bar{B}^0_S\rangle$$

$$|B^0_{S,H}\rangle = p|B^0_S\rangle - q|\bar{B}^0_S\rangle$$

Light, CP-even, shortlived in SM

Heavy, CP-odd, longlived in SM

Three final states:

$J/\psi \phi$  in an S wave

$J/\psi \phi$  in a D wave

$J/\psi \phi$  in a P wave

CP Even

CP Even

CP Odd

A supposedly CP even initial state decays to a supposedly CP odd final state.... like the neutral kaons

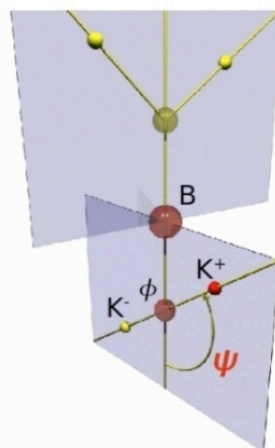
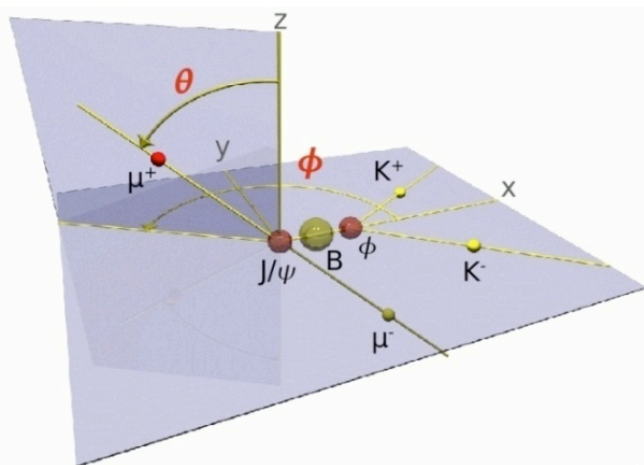


The polarization of the two vector mesons in the decay evolves with a frequency of  $\Delta m_s$

*Measurement needs  $\Delta\Gamma \neq 0$  but not flavor tagging.*

*Measurement needs flavor tagging, resolution, and knowledge of  $\Delta m_s$*

The measurement is a flavor-tagged analysis of time-dependent angular distributions:



$$\hat{n} = (\sin \theta \cos \varphi, \sin \theta \sin \phi, \cos \theta)$$

$$\vec{A}(t, \psi) = (A_0(t) \cos \psi, \frac{-A_{\parallel}(t) \sin \psi}{\sqrt{2}}, i \frac{A_{\perp}(t)}{\sqrt{2}})$$

$$P(\theta, \phi, \psi, t) = \frac{9}{16\pi} |\vec{A}(t, \psi) \times \hat{n}|^2$$

An analysis of an oscillating polarization. 

We measure:

The CP phase  $\beta_s$

Width difference  $\Delta\Gamma_s$  in  $B_s^0$  system (as predicted by HQET)

Lifetime of  $B_s^0$  ( $\tau_s/\tau_0 = 1.00 \pm 0.01$  in HQET)

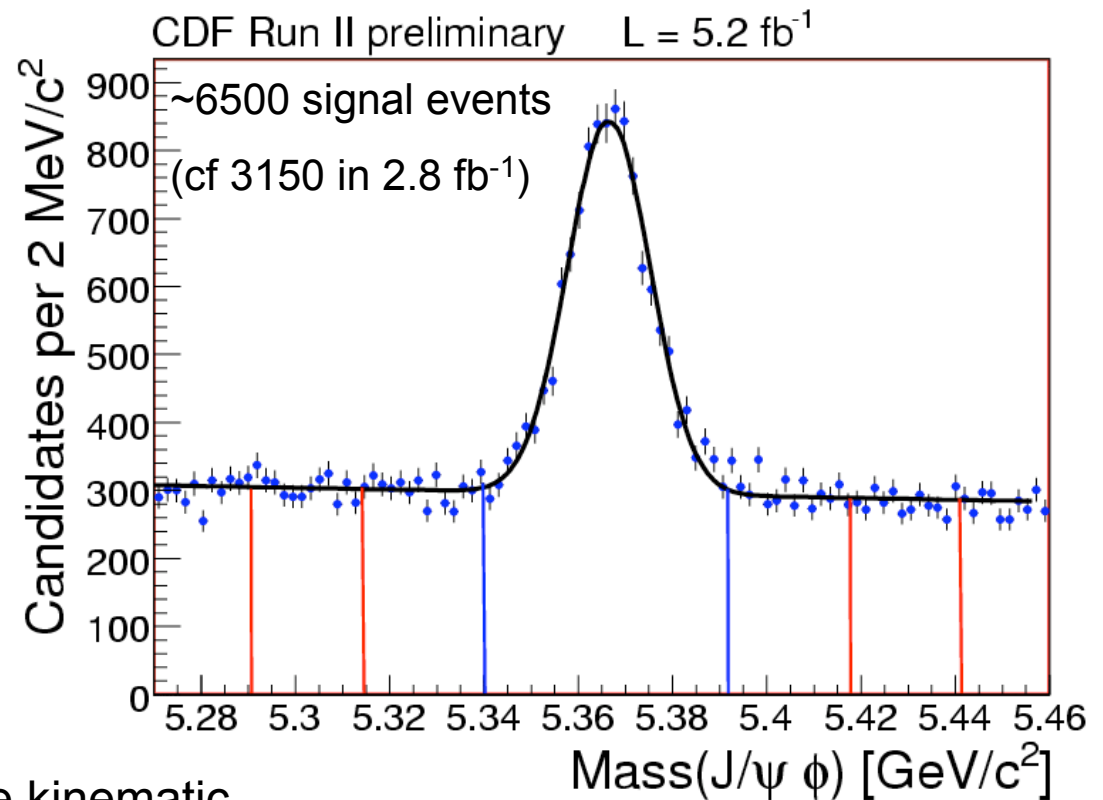
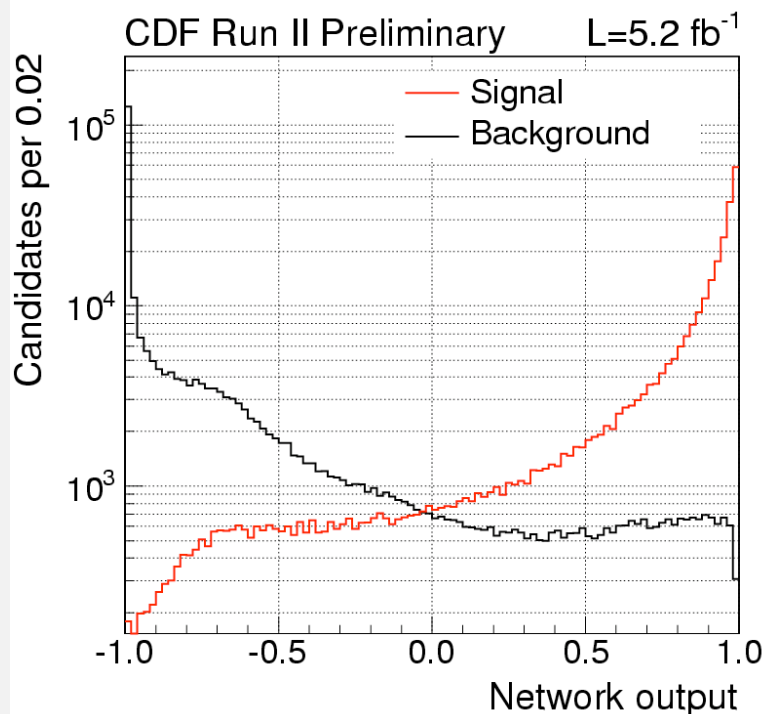
Polarization amplitudes and phases  $A_0, A_{\perp}, A_{\parallel}, \delta_{\perp}, \delta_{\parallel}$

New: in this measurement we incorporate potential contamination from  $B_s^0 \rightarrow J/\psi K^+K^-$  ( $K^+K^-$  in an S-wave) the impact on our results was pointed out by Stone and Zhang Phys. Rev. D 79, 074024 (2009)



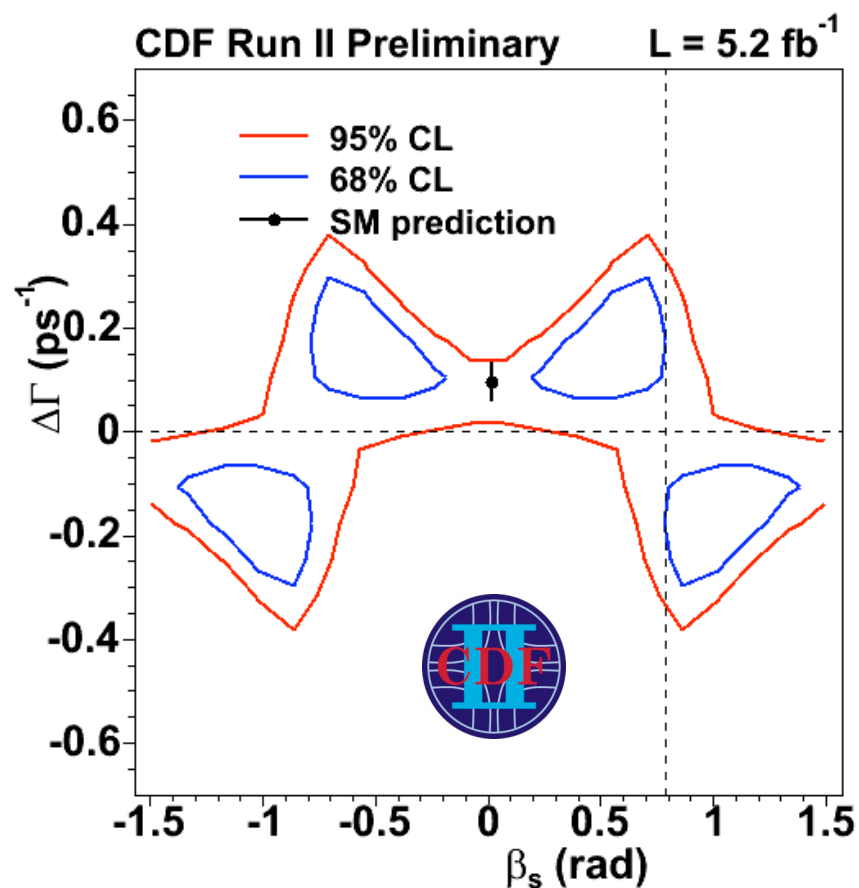
# Data sample.

Event selection by neural network; the cut is optimized by choosing the best statistical error on  $\beta_s$ .



- Neural network inputs include kinematic variables as well as particle ID (TOF and dEdx).
- \*Optimized to minimize the error on  $\beta_s$ .

# Constraints on $\beta_s$ and $\Delta\Gamma_s$ without flavor tagging



Next, we add flavor tagging, the determination of whether the strange bottom meson was born as a  $B^0_s$  or a  $\bar{B}^0_s$ .

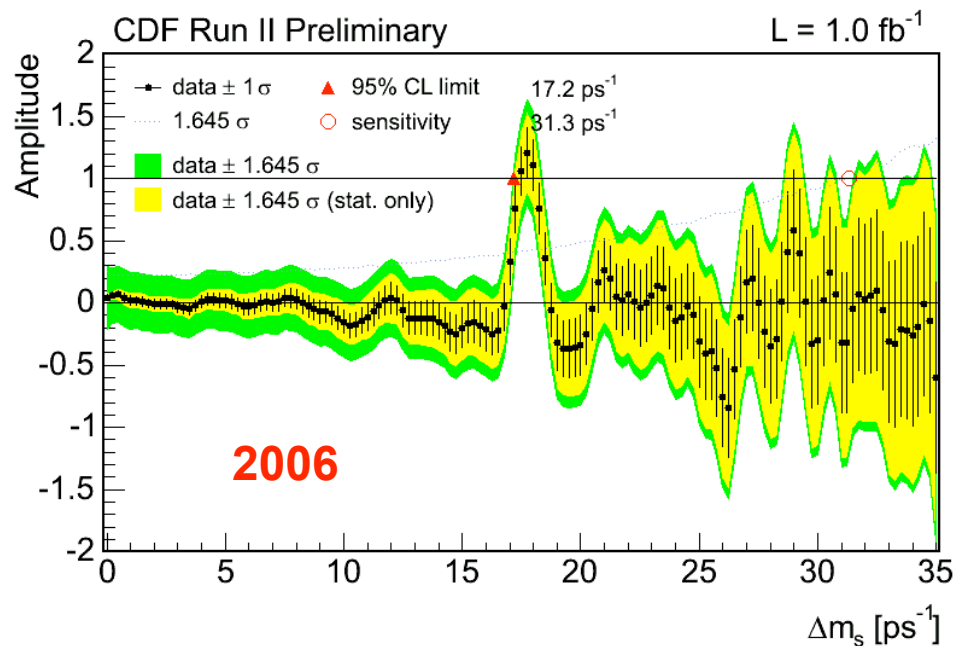
Two varieties of flavor tagging are applied:

OST: “Opposite side tagging”  
 $\epsilon D^2 \sim 1.8\%$  *calibrated using fully reconstructed  $B^\pm$  decays.*

SSKT: “Same side kaon tagging”  
 $\epsilon D^2 \sim 3.2\%$  *calibrated using  $B^0_s$  hadronic decays*



# Same-side Kaon tagging calibrated for the first time since 2006 using $B_s^0$ oscillations



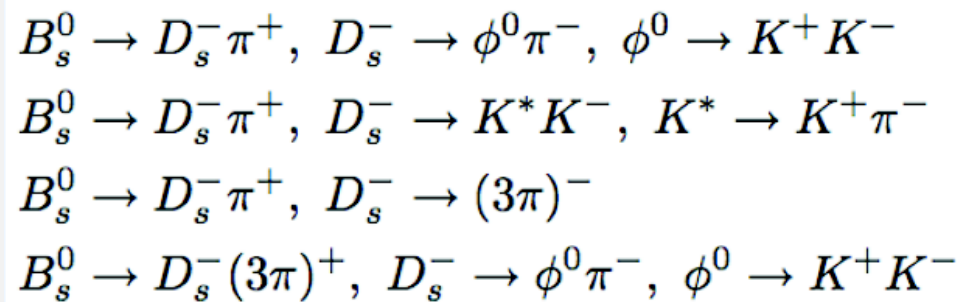
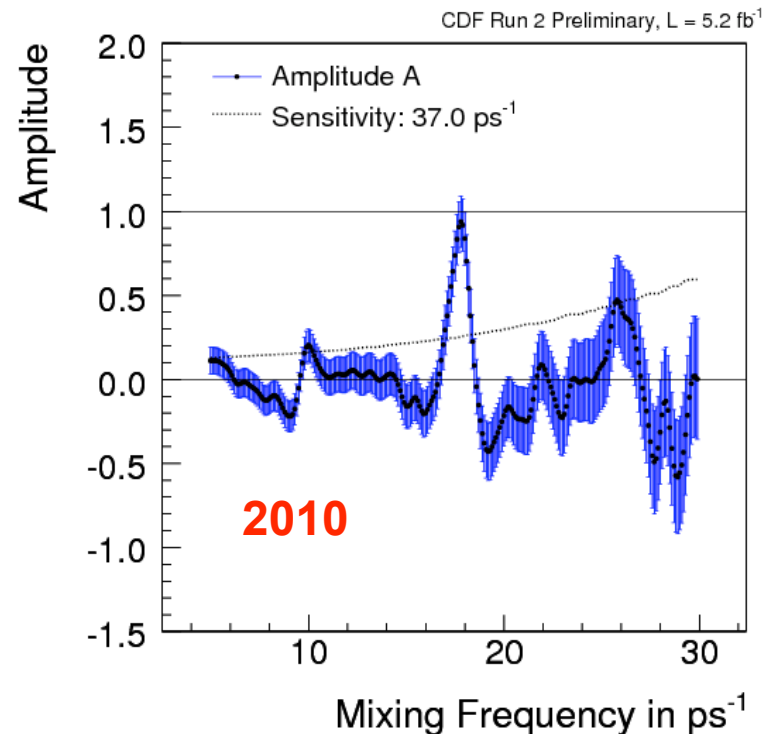
$$A = 0.94 \pm 0.15 \text{ (stat.)} \pm 0.13 \text{ (syst.)}$$

$$T = \varepsilon A^2 D^2 = (3.2 \pm 1.4 \text{ (stat.+syst.)}) \%$$

The measured physical quantities are in agreement with previous measurements:

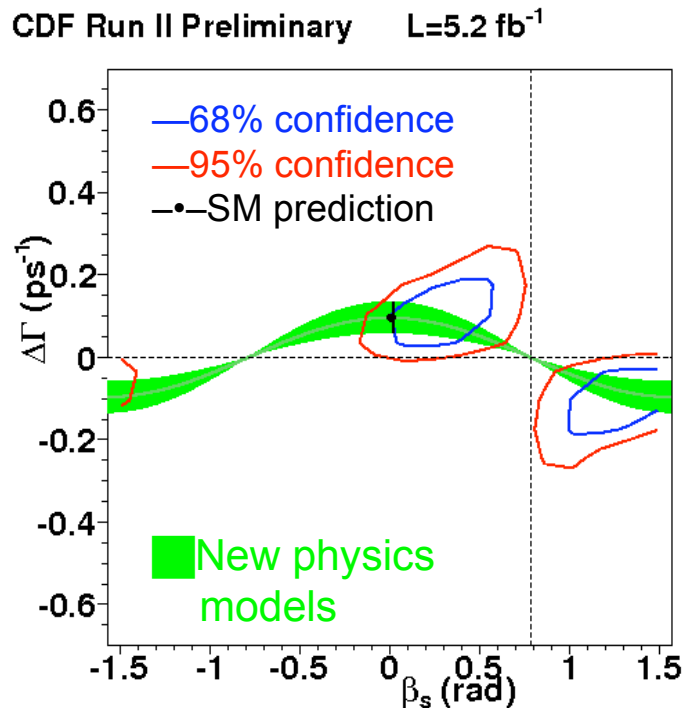
$$c\tau = 451.2 \pm 5.5 \text{ (stat.) } \mu\text{m}$$

$$\Delta m_s = 17.79 \pm 0.07 \text{ (stat.)}$$

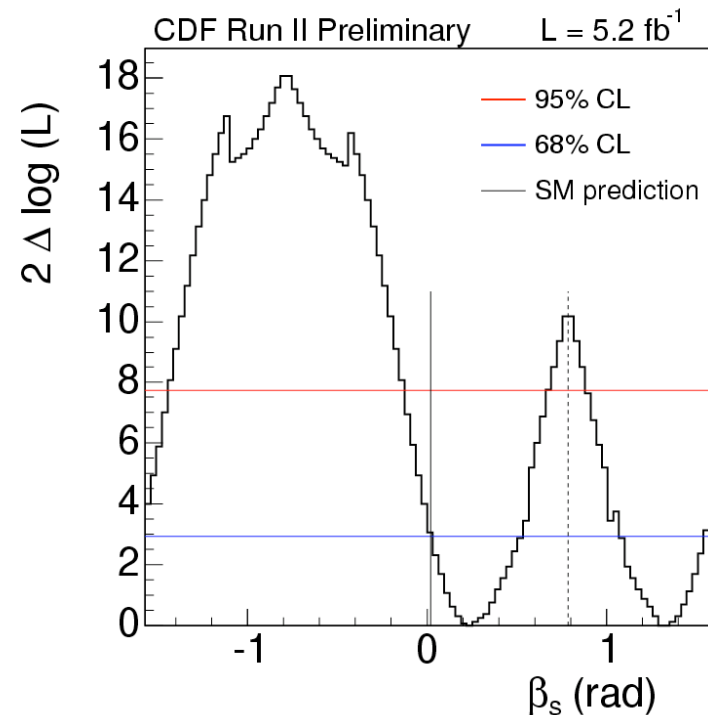




# Results:

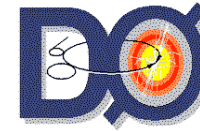


Comparing the green region with the contour tests the computation of  $\Gamma_{12}$  under the hypothesis of mixing induced CP violation independent of the value of  $\beta_s$

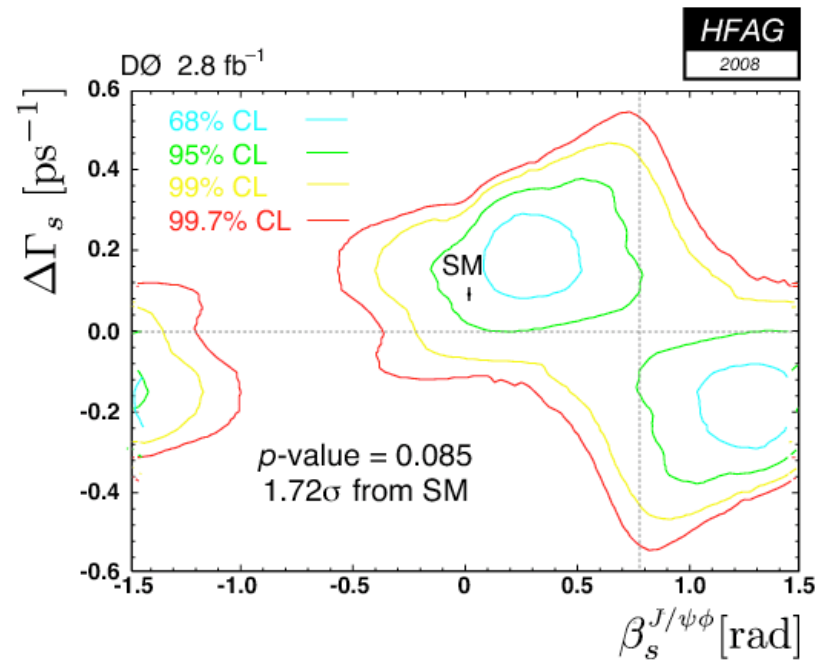
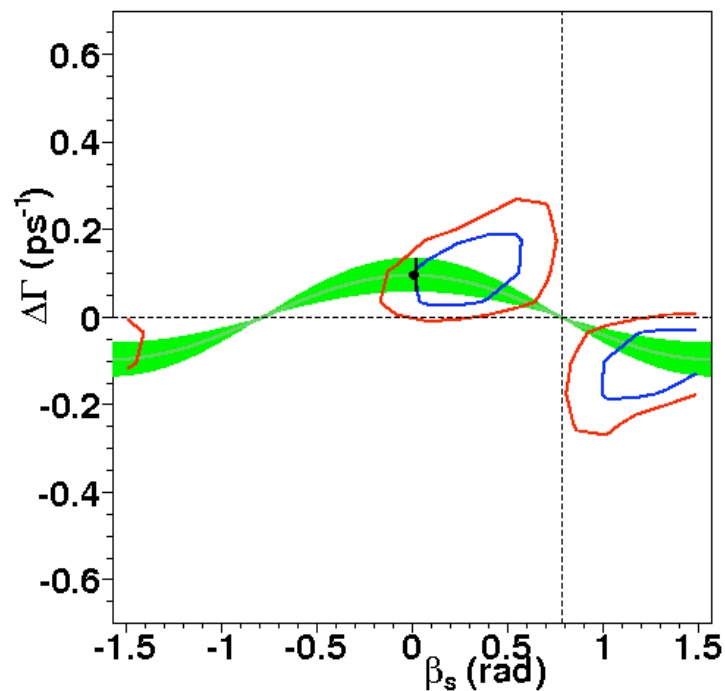


Comparing the confidence intervals in  $\beta_s$  with the Standard Model value value of  $\beta_s=0.019$  tests for new sources of CP violation: we are  $\sim 1\sigma$  from the standard model  $\Rightarrow$  no sign of new physics yet.

D0 are also in the game, but no update since 2.8 fb<sup>-1</sup>

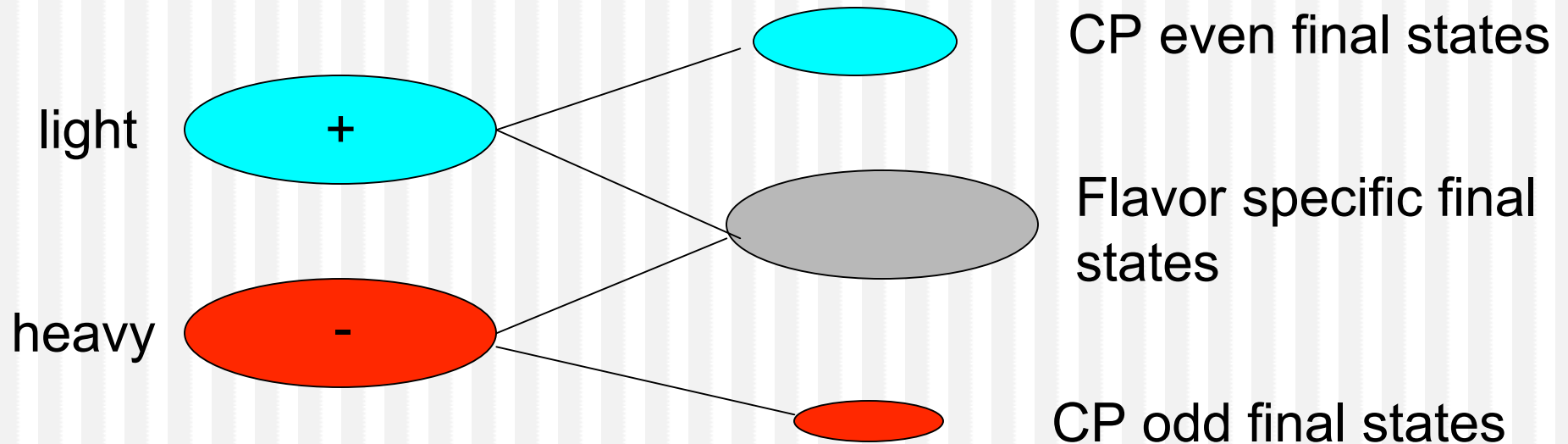


CDF Run II Preliminary L=5.2 fb<sup>-1</sup>

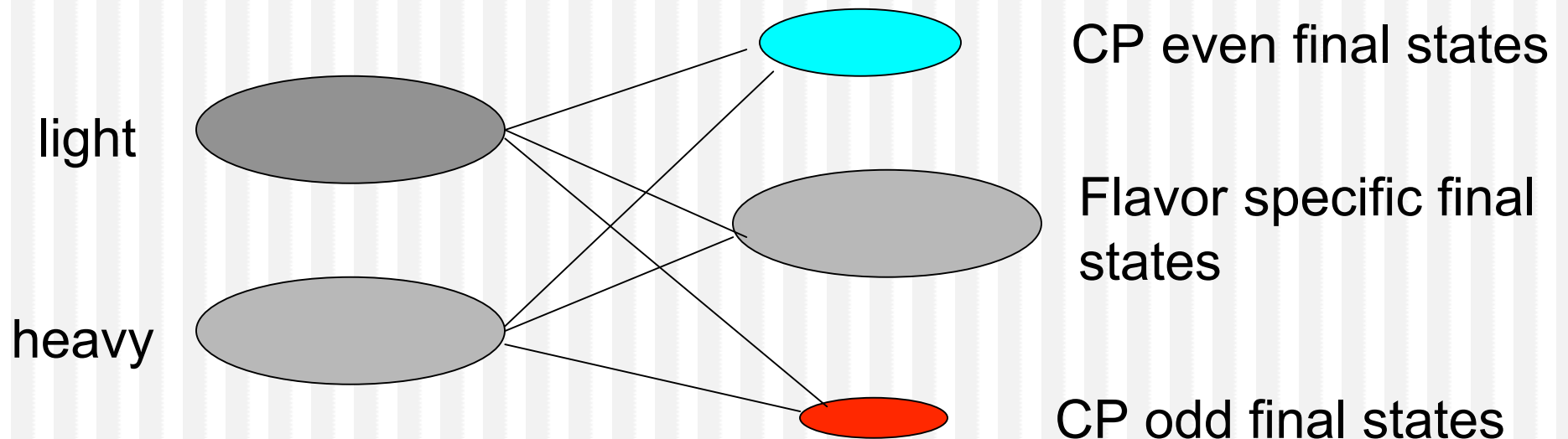




$\Delta\Gamma$  and  $\beta_s$

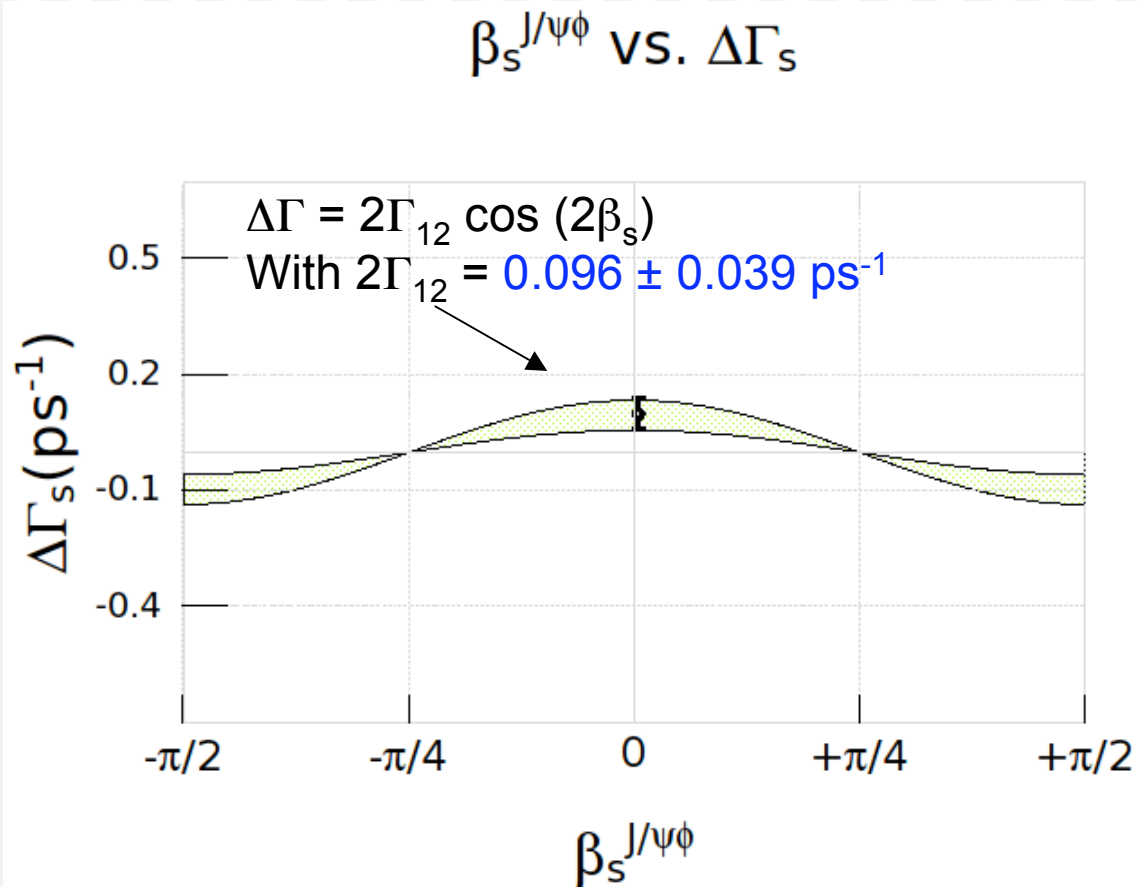


As we turn up Mixing-Induced CP violation ( $\phi_s, -2\beta_s$  in the SM), the two mass eigenstates become equally mixed CP odd and even states:



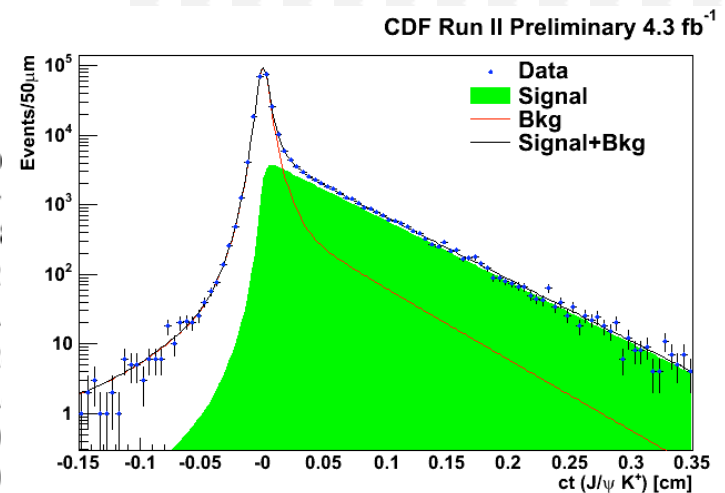
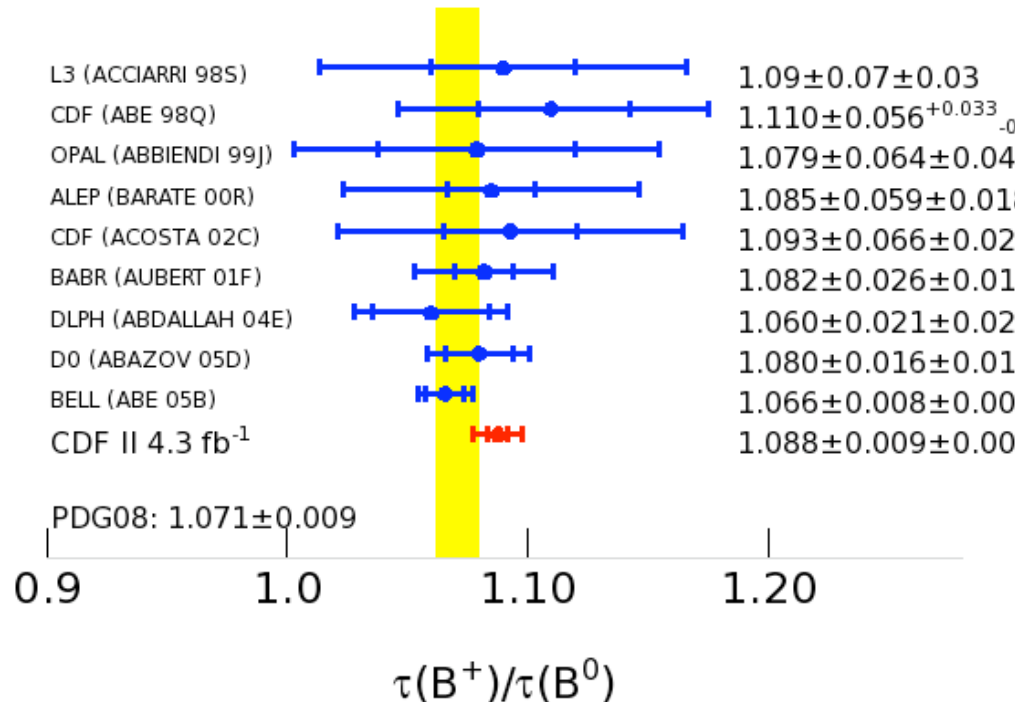


Mixing induced CP violation  
with  $\Gamma_{12}$  from HQE implies constraint on  $\Delta\Gamma$  &  $\beta_s$



$\Gamma_{12}^s$  is an important quantity, it predicts band of values for  $\Delta\Gamma$ ,  $\beta_s$ . The HQE used can be checked in lifetime ratios:

$\tau(B^+)/\tau(B^0)$  measurements



PDG world average and new CDF measurements in  $B^+ \rightarrow J/\psi K^+$ ,  $B^+ \rightarrow J/\psi K^0$

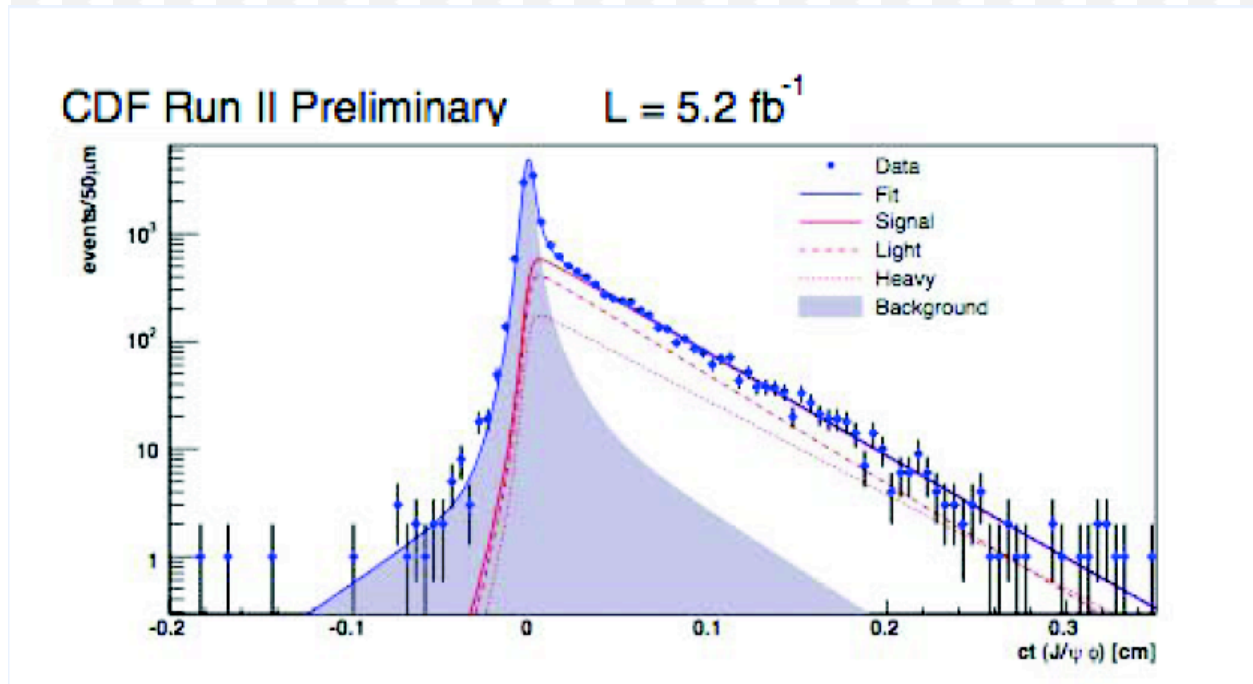
<http://www-cdf.fnal.gov/physics/new/bottom/091217.blessed-jpsix4.3/jpsix.html>

in good agreement with HQE

Theory prediction  $1.063 \pm 0.027$  for this ratio.

Alexander Lenz arXiv:0802.0977

The  $B^0_s$  lifetime  $\tau_s$  is another check of the HQE. The  $B^0_s \rightarrow J/\psi \phi$  analysis also contains the world's best measurement of  $\tau_s$ , predicted to be equal to the  $B^0$  lifetime  $\tau_0$  to within 1%.



$$ct_s = 458.7 \pm 7.5 \text{ (stat)} \pm 3.6 \text{ (syst)} \mu\text{m}$$

$$\Delta\Gamma_s = 0.075 \pm 0.035 \text{ (stat)} \pm 0.01 \text{ (syst)} \text{ ps}^{-1}$$

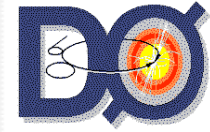
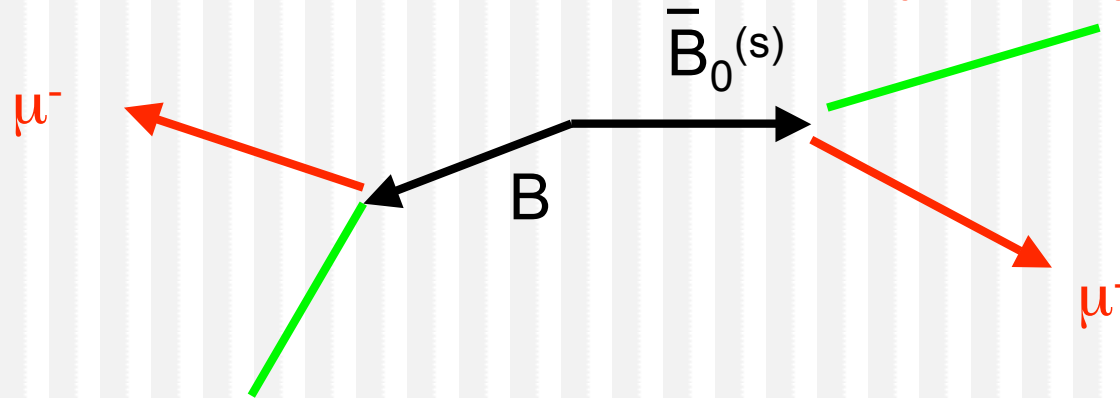
compare  $ct_0 = (459 \pm 2.7 \mu\text{m}, \text{PDG2008})$   
 compare theory  $\Delta\Gamma_s = 0.096 \pm 0.039 \text{ ps}^{-1}$   
 Lenz & Nierste JHEP0706:072,2007

$$|A_{||}(0)|^2 = 0.231 \pm 0.014 \text{ (stat)} \pm 0.015 \text{ (syst)}$$

$$|A_0(0)|^2 = 0.524 \pm 0.013 \text{ (stat)} \pm 0.015 \text{ (syst)}$$

$$\phi_{\perp} = 2.95 \pm 0.64 \text{ (stat)} \pm 0.07 \text{ (syst)}$$

# Measurement of the semileptonic CP Asymmetry $A_{sl}^b$ in D0



arXiv:1005.2757

Same sign muon pairs come from neutral B hadrons which oscillate into their antiparticles (e.g.  $B_s^0$ , 50% of the time).

An excess of negative muons will occur *if there is more  $b$  than  $\bar{b}$  in the shortlived  $B_{s,L}^0$ , i.e. if  $|q/p| > 1$* . This can happen at a low level, in the standard model.

$$a_{sl}^q = \frac{\Gamma(\bar{B}_q^0(t) \rightarrow \mu^+ X) - \Gamma(B_q^0(t) \rightarrow \mu^- X)}{\Gamma(\bar{B}_q^0(t) \rightarrow \mu^+ X) + \Gamma(B_q^0(t) \rightarrow \mu^- X)} = \frac{1 - |q/p|^4}{1 + |q/p|^4}$$

Both  $B^0$  and  $B_s^0$  contribute, at the Tevatron; experimentally one measures

$$\begin{aligned} A_{sl}^b &= (0.506 \pm 0.043) a_{sl}^d + (0.494 \pm 0.043) a_{sl}^s \\ &= (-2.3^{+0.5}_{-0.6}) \times 10^{-4} \text{ using inputs from Lenz \& Nierste hep-ph/0612167} \end{aligned}$$

You will notice that this mechanism depends on the existence of a decay width difference:

$$a_{sl}^q = \frac{\Gamma_q^{12}}{M_q^{12}} \cdot \sin \phi_q = (49.7 \pm 9.4) \times 10^{-4} \sin \phi_q \quad (\text{hep-ph/0612167})$$

$$\phi_s \approx -2\beta_s$$

Like-sign dimuon charge asymmetry

$$A = \frac{N^{++} - N^{--}}{N^{++} + N^{--}}$$

$N^{++}(N^{--})$ : number positive (negative) dimuon events.  
(Definition includes b-hadrons and backgrounds)

Inclusive muon charge asymmetry

$$a = \frac{n^+ - n^-}{n^+ + n^-}$$

$n^+(n^-)$ : number positive (negative) inclusive muons  
(Definition includes b-hadrons and backgrounds)

*These two quantities are measured, then related to  $A_{sl}^b$*

$1.495 \times 10^9$  inclusive muons

$$a = (0.955 \pm 0.003)\%$$

$$a = k A_{sl}^b + a_{bkg}$$
$$A = K A_{sl}^b + A_{bkg}$$

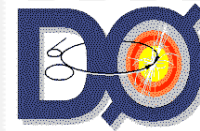
$3.371 \times 10^6$  dimuons

$$A = (0.564 \pm 0.053)\%$$

$$a_{bkg} = f_k a_k + f_\pi a_\pi + f_p a_p + (1 - f_{bkg}) \delta$$

$$A_{bkg} = F_k A_k + F_\pi A_\pi + F_p A_p + (2 - F_{bkg}) \Delta$$

K and k are not unity  
Because of decays  
like  $b \rightarrow c \rightarrow \mu^+$   
Their value is taken  
from simulation.



Kaon asymmetries  $a_k$ ,  $A_k$  from data ( $K^{*0} \rightarrow K^+ \pi^-$  and  $\phi \rightarrow K^+ K^-$ )

Pion and proton asymmetries  $a_\pi$ ,  $A_\pi$ ,  $a_p$ ,  $A_p$  from data ( $K_s^0 \rightarrow \pi^+ \pi^-$  and  $\Lambda^0 \rightarrow p \pi^-$ )

.. where charged tracks satisfy muon selection cuts.

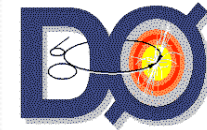
*Kaon fractions  $f_k$ ,  $F_k$  from analysis of  $K^{*0} \rightarrow K^+ \pi^-$  and  $K^{*+} \rightarrow K_s^0 \pi^+$ .*

*Pion and proton fractions  $f_\pi$ ,  $F_\pi$ ,  $f_p$ ,  $F_p$  from  $f_k$ ,  $F_k$  with additional input from Monte Carlo on  $n_\pi/n_K$  and  $n_p/n_K$*

*Muon reconstruction asymmetries  $\delta$  and  $\Delta$  from  $J/\psi \rightarrow \mu^+ \mu^-$  events.*

# Dimuon charge asymmetry

$$A_{sl}^b = (-0.957 \pm 0.251(\text{stat}) \pm 0.146(\text{syst}))\%$$



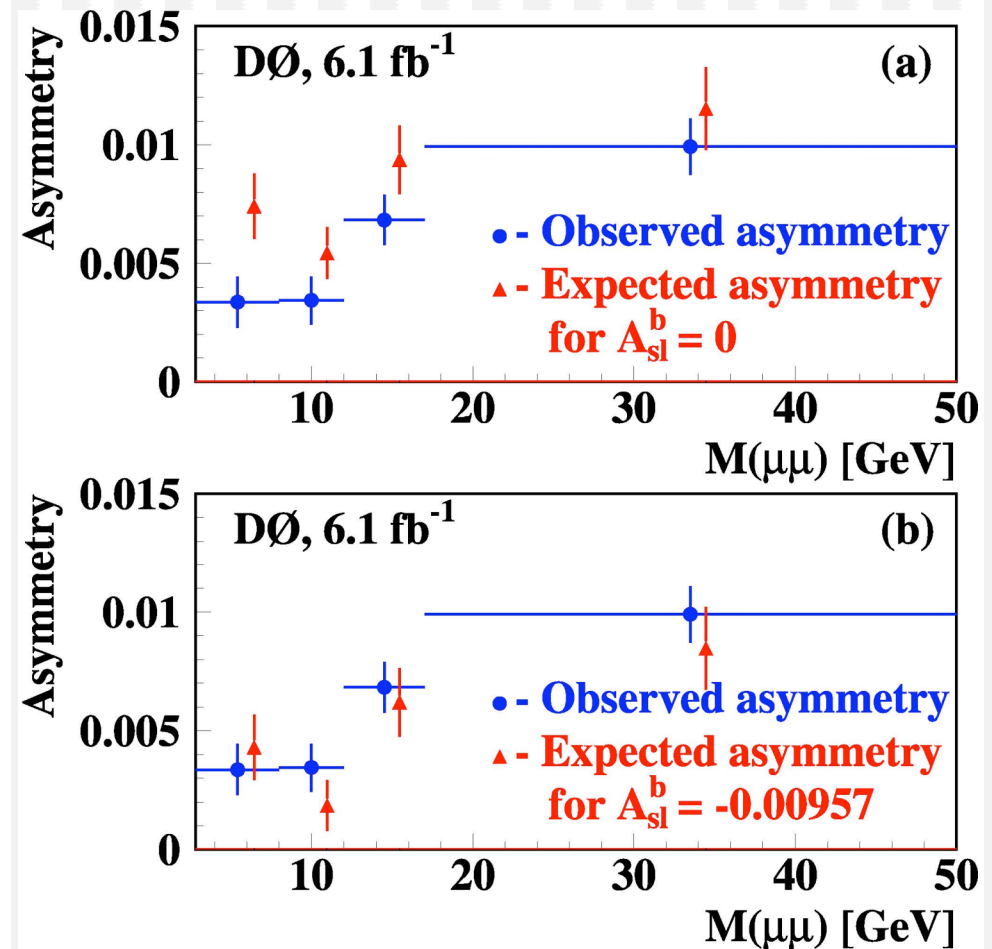
$$A_{sl}^b(\text{SM}) = (-0.023^{+0.005}_{-0.006})\%$$

Discrepancy  
at the  $3.2 \sigma$   
level.

Compare CDF,  $1.6 \text{ fb}^{-1}$ :

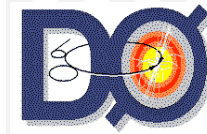
$$A_{sl}^b = (0.80 \pm 0.90(\text{stat}) \pm 0.68(\text{syst}))\%$$

DØ then goes on to  
Interpret the discrepancy  
As an anomalous value of  
 $a_{sl}^s$  from an anomalously high value of  $\phi_s$  as we shall see ➡





# Extract $a_{sl}^s$

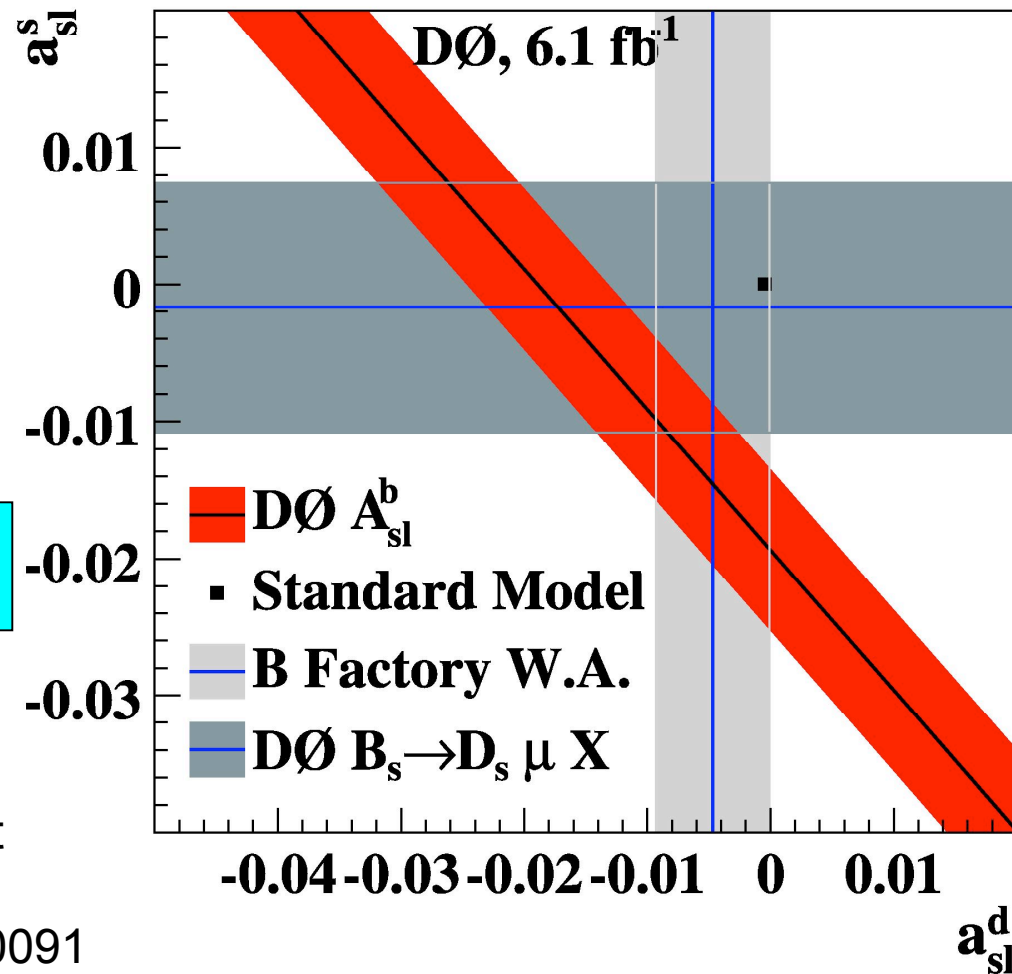


$a_{sl}^s$  is then extracted using additional input from the b-factories on  $a_{sl}^d$ , and Tevatron measurements of fragmentation fractions:

$$a_{sl}^s = (-1.46 \pm 0.75)\%$$

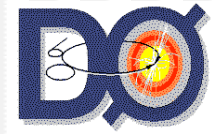
$$a_{sl}^s(SM) = (+0.0021 \pm 0.0006)\%$$

Result consistent with Independent D0 measurement  
Using partially reconstructed  $B_s^0$  decays:  $a_{sl}^s = -0.0017 \pm 0.0091$   
arXiv:0904.3907





# Extract bounds on $\phi_s, \Delta\Gamma$



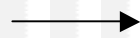
Bounds on  $\phi_s$  and  $\Delta\Gamma$  are extracted with the assumption of mixing-induced CP violation:

Take

$$a_{sl}^q = \frac{\Gamma_q^{12}}{M_q^{12}} \cdot \sin \phi_q$$

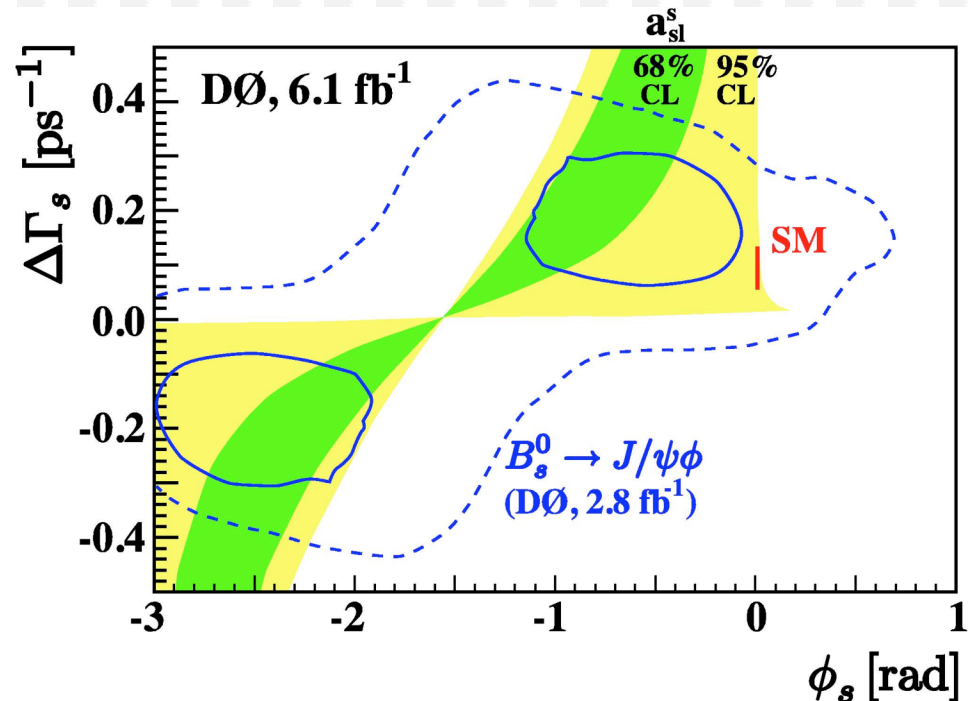
$$\Delta M_s = 2|M^{12}|$$

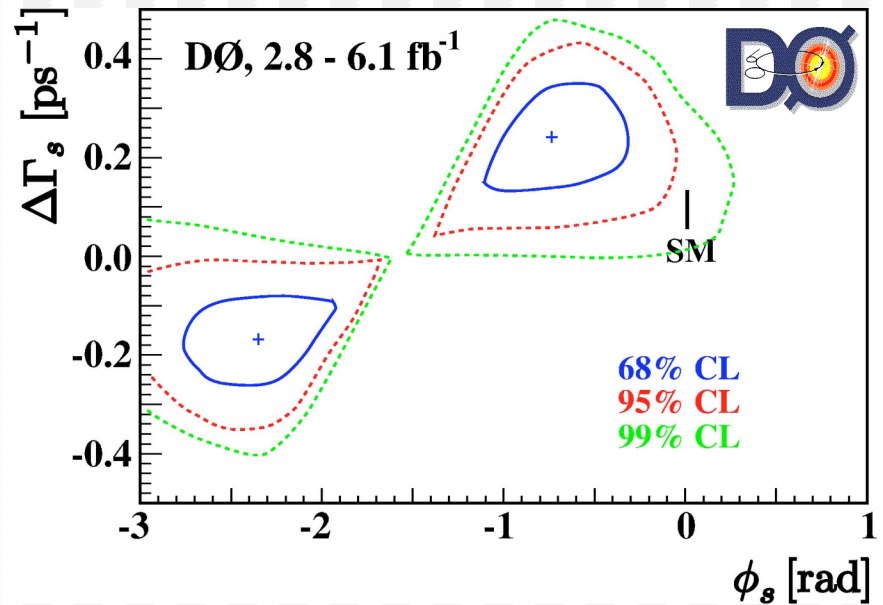
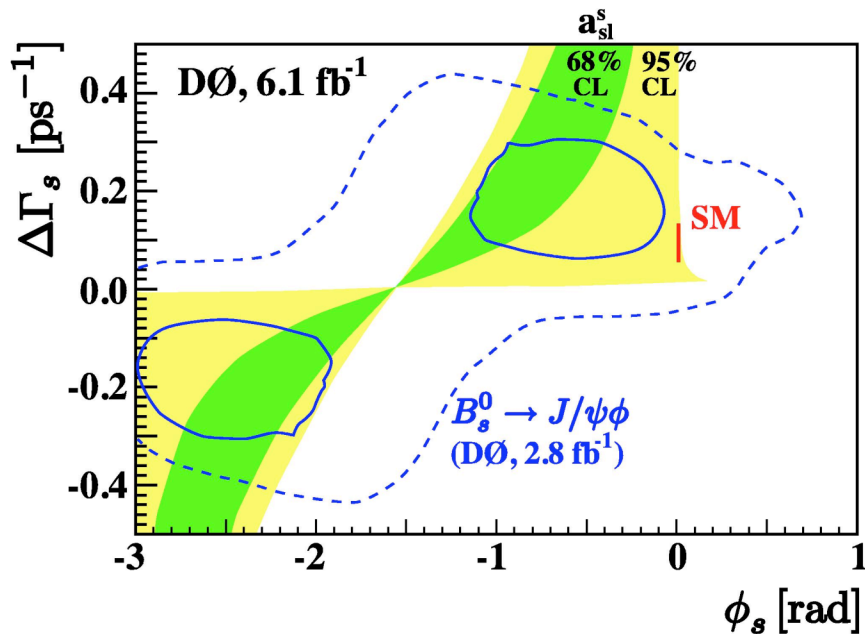
$$\Delta\Gamma_s = 2|\Gamma^{12}| \cdot \cos \phi_s$$



$$a_{sl}^s = \frac{\Delta\Gamma_q}{\Delta M_q} \cdot \tan \phi_s$$

(Reminder, this is the condition of Mixing induced CP violation!)





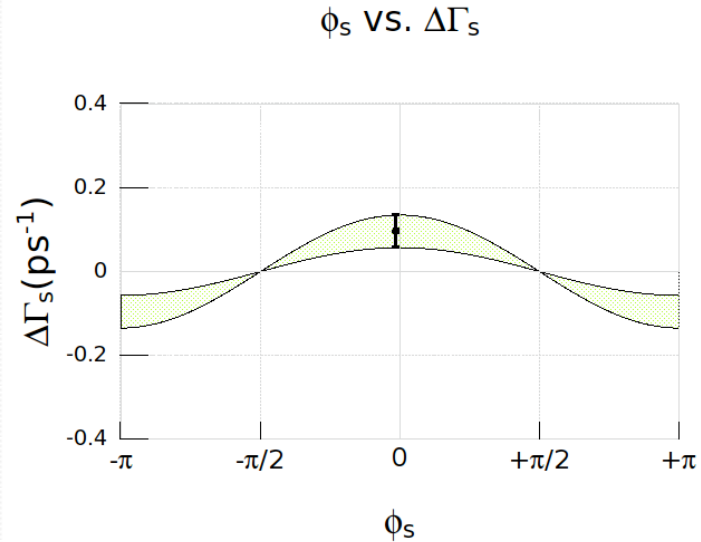
The D0 analysis of  $J/\psi \phi$  and the D0 muon asymmetries are consistent and can be combined in the context of Mixing Induced CP Violation.

But then one can compare this with theoretical predictions of  $\Gamma_{12}$ , which also imply bounds in the same parameter space, and there is some tension because:

$$a_{sl}^q = \frac{\Gamma_q^{12}}{M_q^{12}} \cdot \sin \phi_q = (49.7 \pm 9.4) \times 10^{-4} \sin \phi_q$$

compare

$$a_{sl}^s = (-1.46 \pm 0.75)\%$$



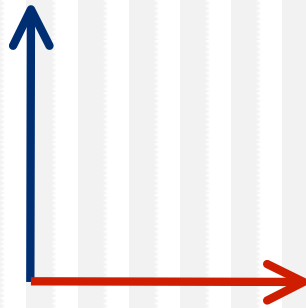
See Bauer & Dunn arXiv:1006.1629 for comments on new physics contributions to  $\Gamma_{12}$

# Conclusions

- CDF reports an updated measurement of the CP violating phase  $\beta_s$ , now more precise and consistent with the standard model at  $\sim 1\sigma$  level.
- D0 reports a 3.2 sigma anomaly in the semileptonic CP asymmetry  $A_{sl}^b$ .
- In the context of Mixing Induced CP violation:
  - The  $\beta_s$  measurements (CDF,D0) are consistent with hypothesis.
  - The D0  $a_{sl}^s$  measurement is consistent with the  $\beta_s$  measurements
  - The  $a_{sl}^s$  measurements seems to center in an unphysical region, but maybe OK within errors for the highest values of  $\beta_s$
  - A certain tension presently exists between the three sources of bounds on  $\beta_s$  and  $\Delta\Gamma$ .
  - LHCb inherits a situation that I personally find a little unclear.



Time dependence of the angular distributions: use a basis of linear polarization states of the two vector mesons  $\{S, P, D\} \rightarrow \{P_{\perp}, P_{||}, P_0\}$



CP odd states decay  
to  $P_{\perp}$

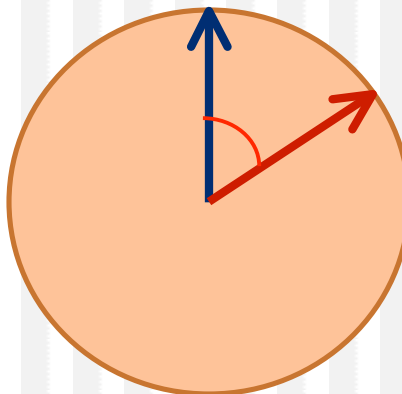


CP even states decay  
to  $P_{||}, P_0$

If  $[H, CP] \neq 0$

Then  $\frac{d}{dt} \langle CP \rangle \neq 0$

$$\Delta m_s \sim 17.77 \text{ ps}^{-1}.$$



- The polarization correlation depends on decay time.

- Angular distribution of decay products of the  $J/\psi$  and the  $\phi$  analyze the rapidly oscillating correlation.



reference material

$$\hat{n} = (\sin \theta \cos \varphi, \sin \theta \sin \varphi, \cos \theta)$$

$$\vec{A}(t) = (A_0(t) \cos \psi, -\frac{A_{\parallel}(t) \sin \psi}{\sqrt{2}}, i \frac{A_{\perp}(t)}{\sqrt{2}})$$

$$P(\theta, \varphi, \psi, t) = \frac{9}{16\pi} |\vec{A}(t) \times \hat{n}|^2$$

$$A_i(t) = \frac{a_i e^{-imt} e^{-\Gamma t/2}}{\sqrt{\tau_H + \tau_L \pm \cos 2\beta_s \cdot (\tau_L - \tau_H)}} [E_+(t) \pm e^{2i\beta'} E_-(t)] \quad \text{B}$$

$$\bar{A}_i(t) = \frac{a_i e^{-imt} e^{-\Gamma t/2}}{\sqrt{\tau_H + \tau_L \pm \cos 2\beta_s \cdot (\tau_L - \tau_H)}} [\pm E_+(t) + e^{-2i\beta_s} E_-(t)] \quad \bar{\text{B}}$$

$$E_{\pm}(t) = \frac{1}{2} \left[ e^{+(\frac{-\Delta\Gamma}{4} + i\frac{\Delta m}{2})t} \pm e^{-(\frac{-\Delta\Gamma}{4} + i\frac{\Delta m}{2})t} \right]$$

These expressions are:

- \* used directly to generate simulated events.
- \* expanded, smeared, and used in a Likelihood function.
- \* summed over B and  $\bar{\text{B}}$  (untagged analysis only)

An analysis of the decay can be done with either a mix of B and  $\bar{\text{B}}$  mesons (untagged) or with a partially separated sample (flavor tagged). Latter is more difficult and more powerful.

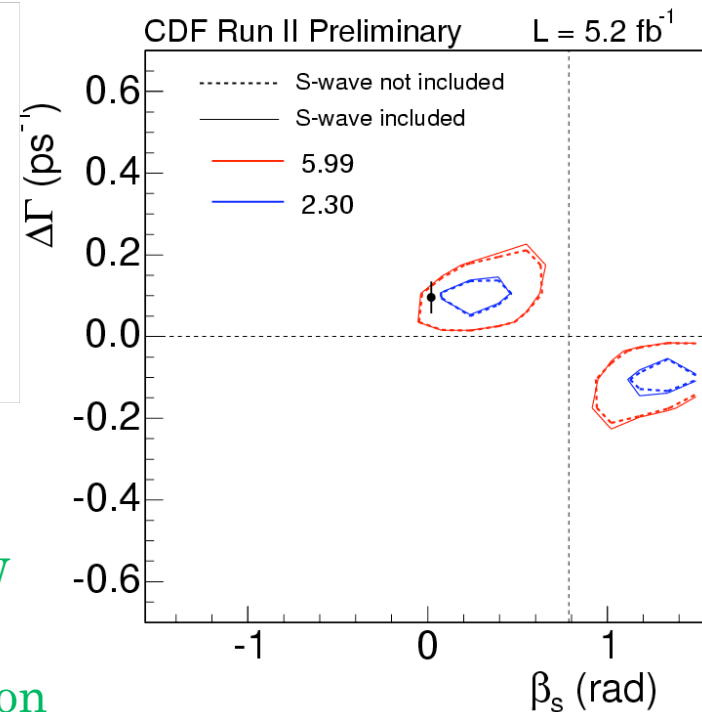
## Modifications to the Likelihood for the S-wave contamination

You also need this for the S-wave component:

$$\vec{B}(t) = (B(t), 0, 0)$$

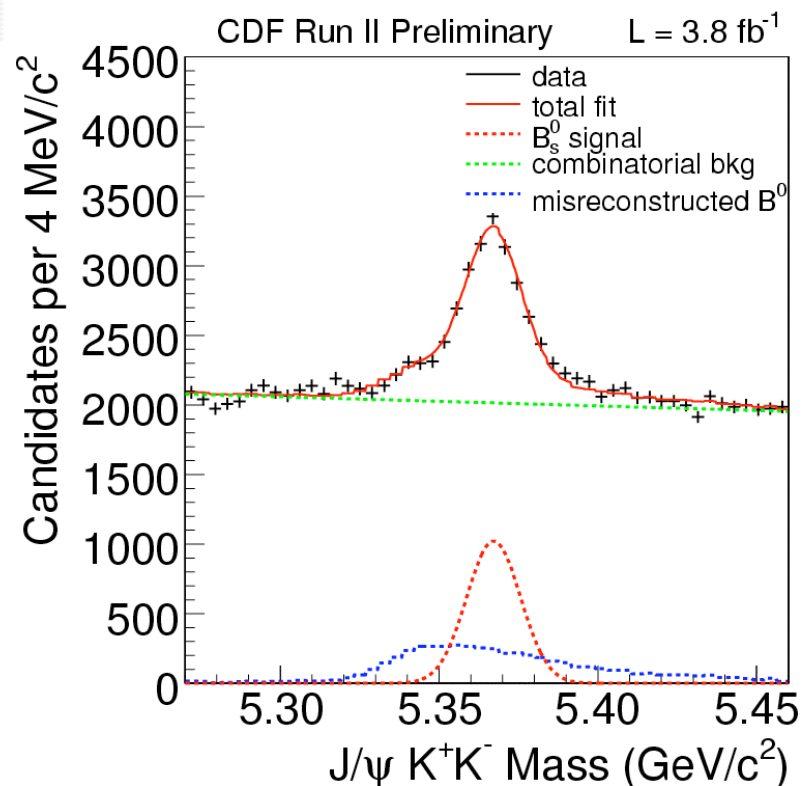
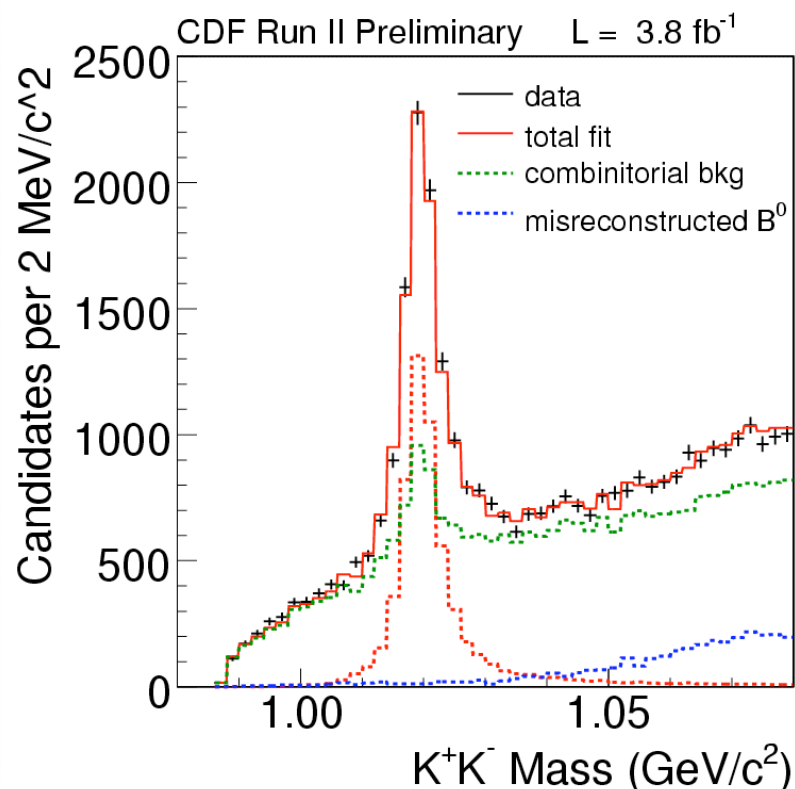
$$Q(\theta, \phi, \psi, t) = \frac{3}{16\pi} |\vec{B}(t) \times \hat{n}|^2$$

- S-wave is pure CP odd
- $\phi$ -mass dependence: nonrelativistic BW
- includes P-wave S-wave interference.
- and the proper detector re-normalization after the detector sculpting.



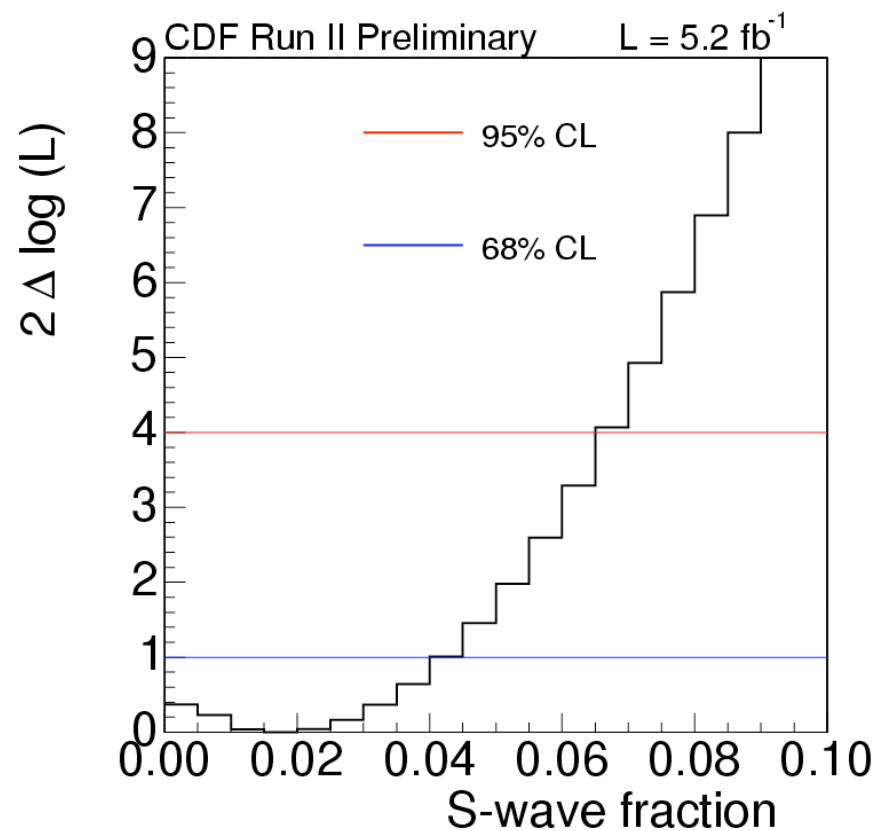
# KK mass shape in the region of the $\phi$

Invariant KK mass (left)  
Combinatorial background from  $B_s^0$  sidebands.  
 $B^0$  reflections: shape from MC,  
Fractions from  $B_s^0$  mass fit (right)





# Fitted S-wave fraction:



Source	$A_{\text{sl}}^b$ inclusive muon	$A_{\text{sl}}^b$ dimuon	$A_{\text{sl}}^b$ combined
$A$ or $a$ (stat)	0.00066	0.00159	0.00179
$f_K$ or $F_K$ (stat)	0.00222	0.00123	0.00140
$P(\pi \rightarrow \mu)/P(K \rightarrow \mu)$	0.00234	0.00038	0.00010
$P(p \rightarrow \mu)/P(K \rightarrow \mu)$	0.00301	0.00044	0.00011
$A_K$	0.00410	0.00076	0.00061
$A_\pi$	0.00699	0.00086	0.00035
$A_p$	0.00478	0.00054	0.00001
$\delta$ or $\Delta$	0.00405	0.00105	0.00077
$f_K$ or $F_K$ (syst)	0.02137	0.00300	0.00128
$\pi, K, p$ multiplicity	0.00098	0.00025	0.00018
$c_b$ or $C_b$	0.00080	0.00046	0.00068
Total statistical	0.01118	0.00266	0.00251
Total systematic	0.02140	0.00305	0.00146
Total	0.02415	0.00405	0.00290

Dominant uncertainties